

From images to descriptors and back again

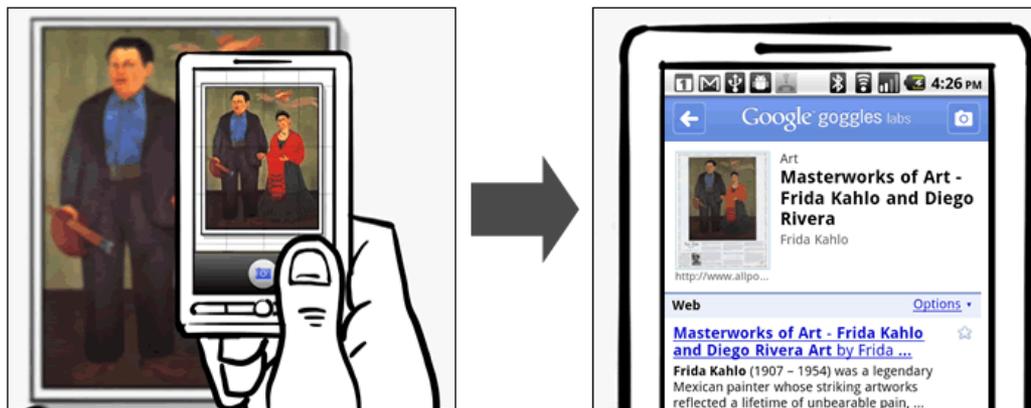
Patrick Pérez



FGMIA 2014

Visual search

- Searching in image and video databases
- One scenario: *query-by-example*
 - Input: one query image
 - Output
 - Ranked list of “relevant” visual content
 - Information on object/scene visible in query
- Some existing systems
 - Google Image and Goggles / Amazon Flow / Kooaba (Qualcom)



Large scale image comparison

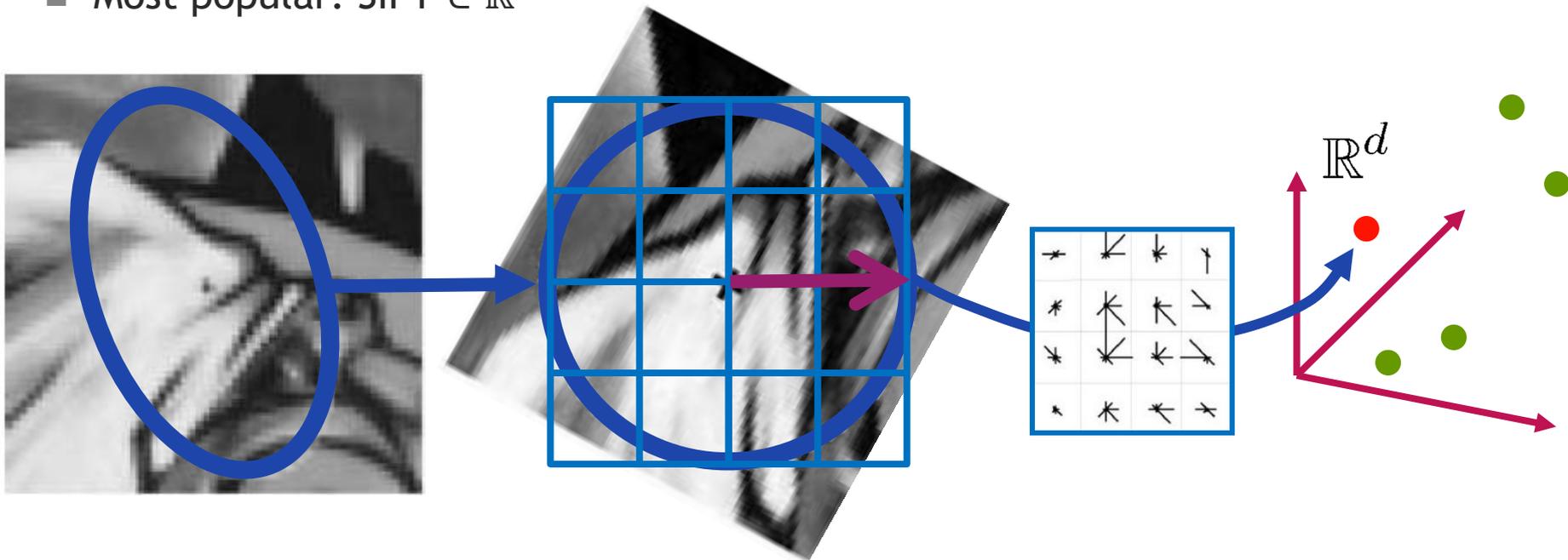
- Raw images can't be compared pixel-wise
 - Relevant information is lost in clutter and changes place
 - No invariance or robustness

- Meaningful and robust representation
 - Global statistics
 - *Local descriptors aggregated in a global signature*

- Efficient approximate comparisons

Local descriptors

- Select/detect image fragments, normalize and describe them
 - Robust to some geometric and photometric changes
 - Most popular: SIFT $\in \mathbb{R}^{128}$



- Precise image comparison: match fragments based on descriptors
 - Works very well ... but way too expensive on a large scale

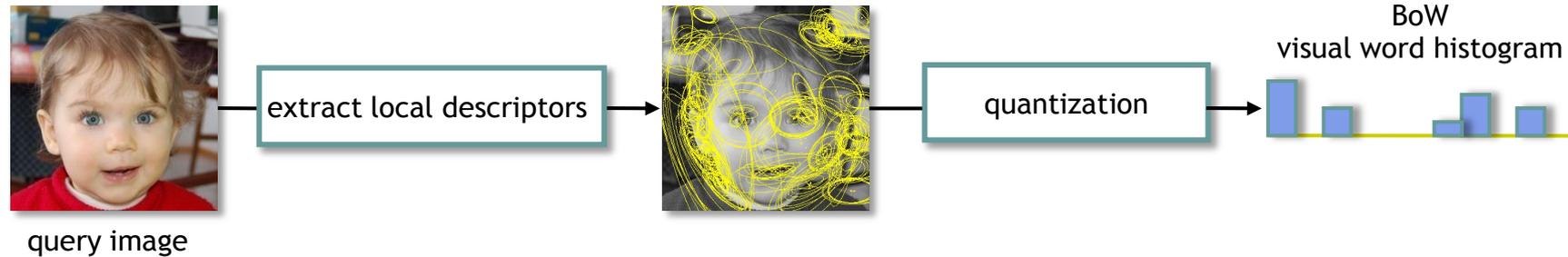
[Mikolajczyk , Schmid. IJCV 2004]

[Lowe. IJCV 2004]

technicolor



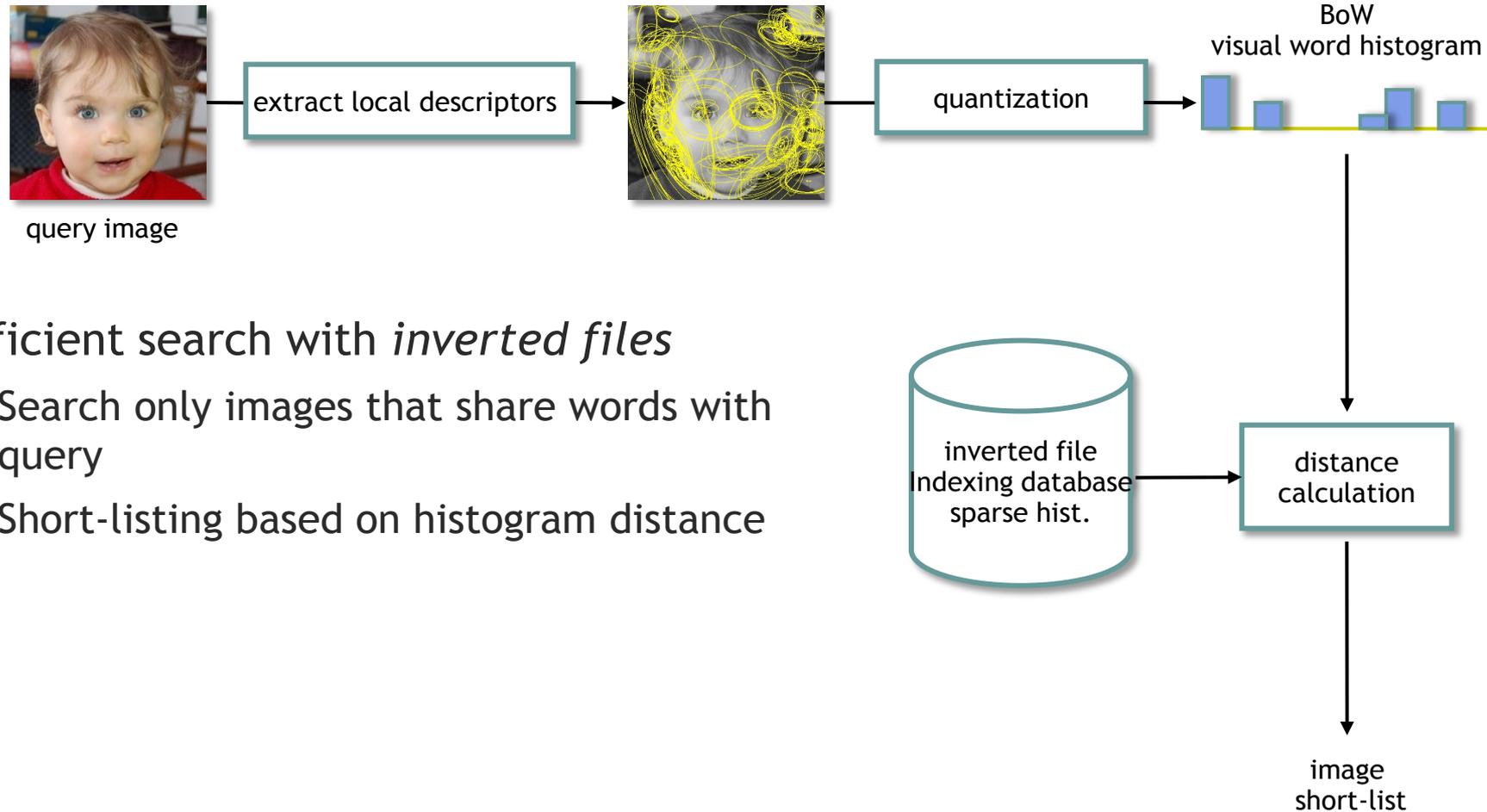
Bag of “Visual Words” pipeline



- Forget about precise descriptors
 - Vector-quantization using a dictionary of k “visual words” learned off-line
- Forget about fragment location
 - Counting visual words
- BoW: *sparse fixed size signature by aggregation* of a variable number of quantized local descriptors

[Sivic, Zisserman. ICCV 2003][Csurca *et al.* 2004]

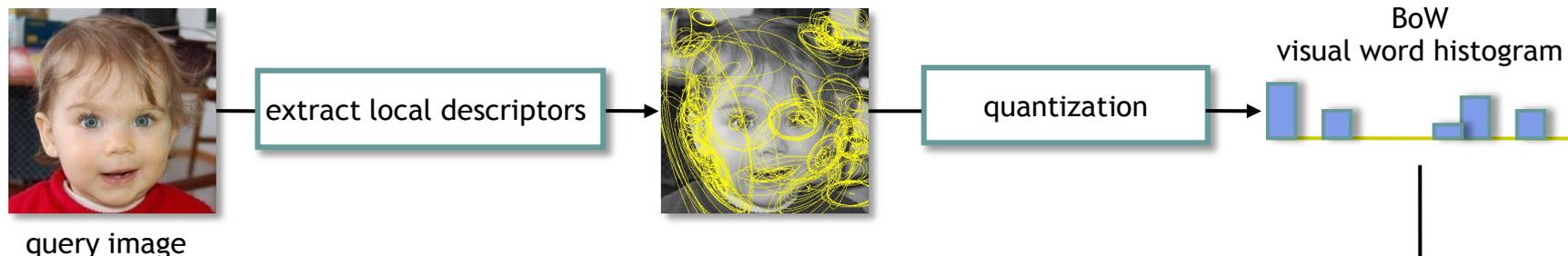
Bag of “Visual Words” pipeline



- Efficient search with *inverted files*
 - Search only images that share words with query
 - Short-listing based on histogram distance

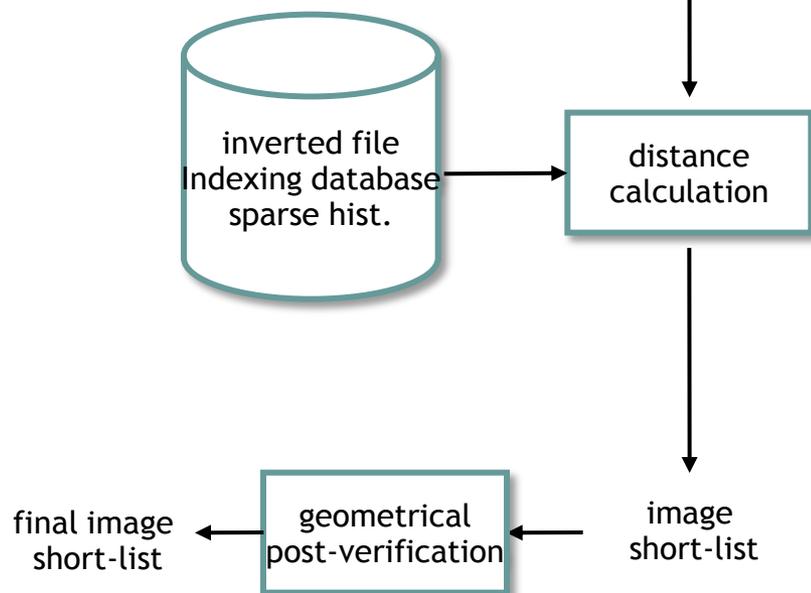
[Sivic, Zisserman. ICCV 2003]

Bag of “Visual Words” pipeline



■ Geometrical post-verification

- Match local features
- Infer most likely geometric transform
- Rank short list based on goodness-of-fit



[Sivic, Zisserman. ICCV 2003]

technicolor



Limitations and contributions

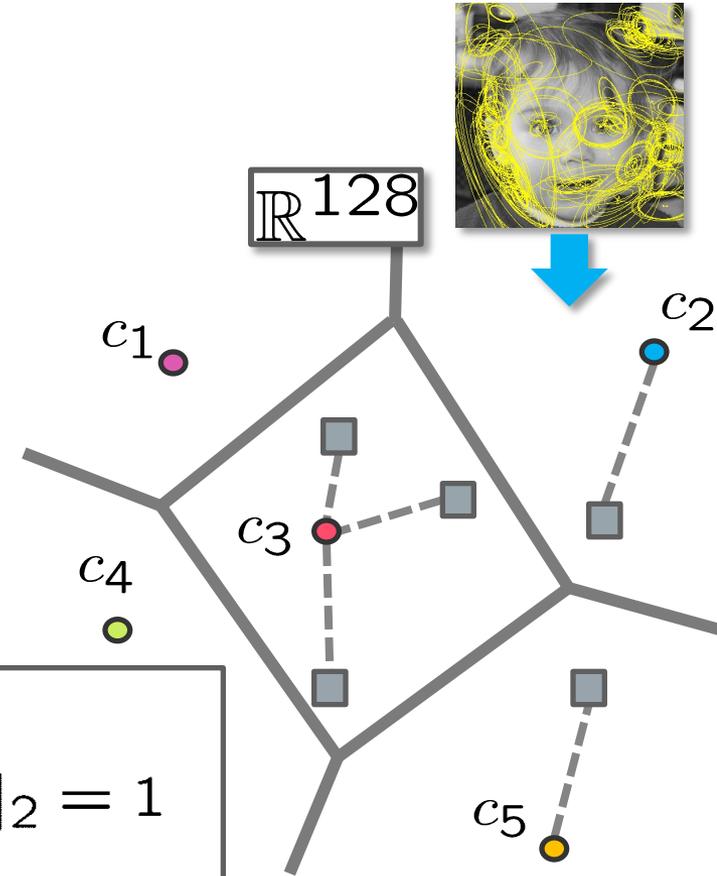
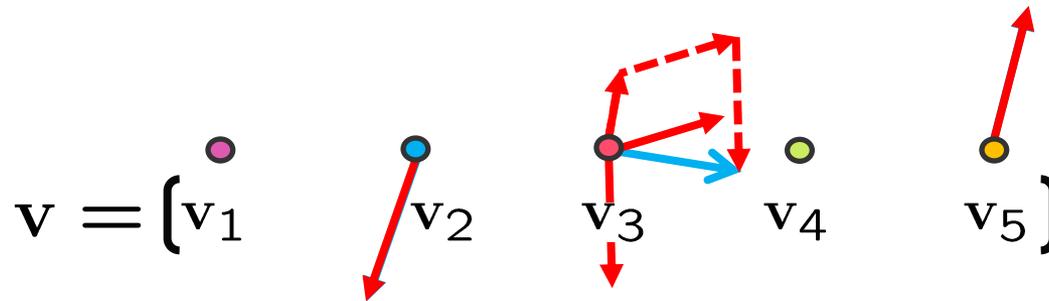
- Precise search requires large dictionary ($k \sim 20,000-200,000$ words)
 - Difficult to learn
 - Costly to compute (k distances per descriptor) on database
 - Memory footprint still too large ($\sim 10\text{KB}$ per image)
 - With 40GB RAM, search 10M images in 2s
 - Does not scale up to web-scale ($\propto 10^{11}$ images)
- Contribution*
 - Novel aggregation of local descriptors into image signature
 - Combined with efficient indexing
 - Low memory footprint (20B per image, 200MB RAM for 10M images)
 - Fast search (50ms to search within 10M images on laptop)

*[Jégou, Douze, Schmid, Pérez. CVPR 2010]

Beyond cell counting

■ Vector of Locally Aggregated Descriptors (VLAD)

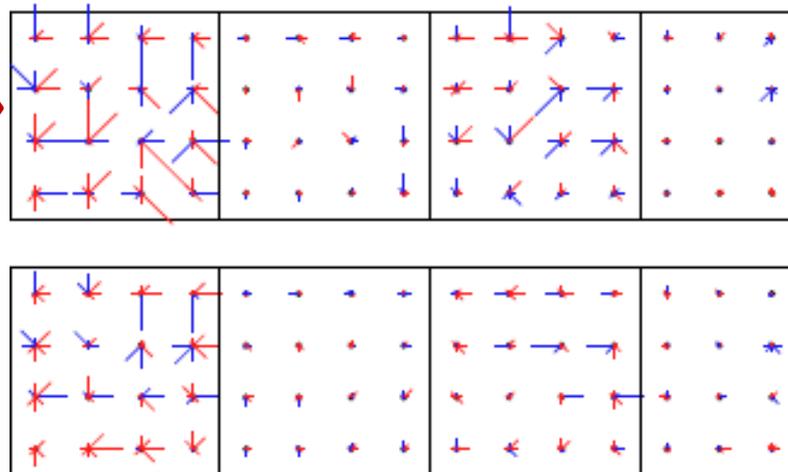
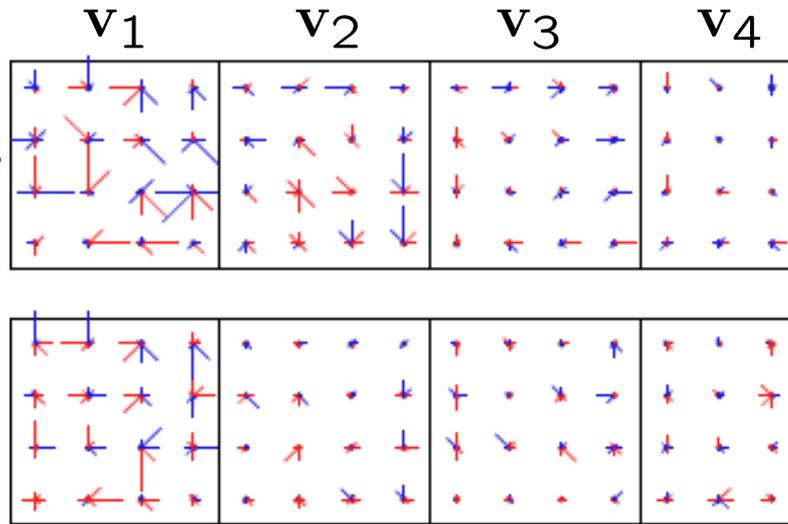
- Very coarse visual dictionary (e.g., $k = 64$): $\mathcal{C} = \{c_1, \dots, c_k\} \in \mathbb{R}^{128}$
- But characterize distribution in each cell



$$\mathbf{v} \propto \begin{bmatrix} v_1 \\ \vdots \\ v_k \end{bmatrix} \in \mathbb{R}^{128k}, \quad v_i = \sum_{\mathbf{x} \in \text{cell } i} (\mathbf{x} - c_i), \quad \|\mathbf{v}\|_2 = 1$$

VLAD

- Vectors of size $D = 128 \times k$, k SIFT-like blocks



Fisher interpretation

- Given parametric family of pdfs $\{p_\theta, \theta \in \Theta \subset \mathbb{R}^u\}$
 - Fisher information matrix (size u)

$$F_\theta = \mathbb{E}_{p_\theta}[\nabla_\theta \ln p_\theta \nabla_\theta^T \ln p_\theta]$$

- Log-likelihood gradient of sample $\{\mathbf{x}_n\}_{n=1\dots N}$

$$G_\theta(\{\mathbf{x}_n\}) = \frac{1}{N} \sum_{j=1}^N \nabla_\theta \ln p_\theta(\mathbf{x}_j)$$

- Fisher kernel: given θ , compare two samples

$$\begin{aligned} K_\theta(\{\mathbf{x}_m\}, \{\mathbf{y}_n\}) &= G_\theta(\{\mathbf{y}_m\})^\top F_\theta^{-1} G_\theta(\{\mathbf{x}_n\}) \\ &= \langle F_\theta^{-\frac{1}{2}} G_\theta(\{\mathbf{y}_m\}), \underbrace{F_\theta^{-\frac{1}{2}} G_\theta(\{\mathbf{x}_n\})}_{\mathcal{G}_\theta(\{\mathbf{x}_n\})} \rangle \end{aligned}$$

- Dot product of *Fisher vectors* (FV)

VLAD and Fisher vector

- Example: spherical GMM with parameters $\theta = (\{\pi_i, \boldsymbol{\mu}_i, \sigma_i\})_{i=1\dots k}$
 - *Approximate* FV on mean vectors only

$$\mathcal{G}_{\boldsymbol{\mu}_i}(\{\mathbf{x}_n\}) = \frac{1}{N\sqrt{\pi_i}} \sum_{n=1}^N \kappa_n(i) \sigma_i^{-1} (\mathbf{x}_n - \boldsymbol{\mu}_i), \quad i = 1 \dots k$$

with *soft assignments* $\kappa_n(i)$. FV of size $D = d \times k$

- If equal weights and variances, hard assignment to code-words, FV = VLAD

$$\mathcal{G}_{\boldsymbol{\mu}_i}(\{\mathbf{x}_n\}) \propto \mathbf{v}_i(\{\mathbf{x}_n\}), \quad i = 1 \dots k$$

Additional tricks

- Power-law¹ $v_j \leftarrow \text{sign}(v_j)|v_j|^\alpha$, $j = 1 \dots D$, $\alpha \in (0, 1)$

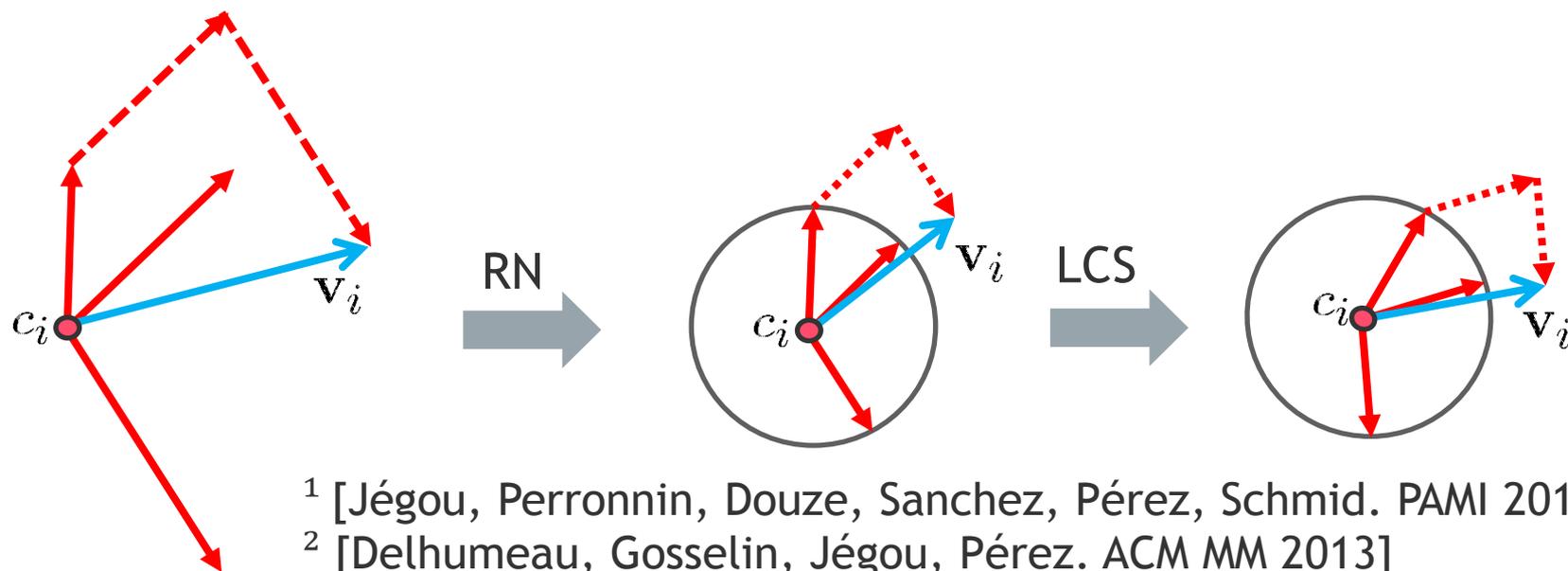
- Residue normalization (“RN”)²

$$\mathbf{v}_i = \sum_{\mathbf{x} \in \text{cell } i} \frac{\mathbf{x} - \mathbf{c}_i}{\|\mathbf{x} - \mathbf{c}_i\|_2}, \quad i = 1 \dots k$$

- Intra-cell PCA local coordinate system (“LCS”)²

$$\mathbf{v}_i = R_i \sum_{\mathbf{x} \in \text{cell } i} \frac{\mathbf{x} - \mathbf{c}_i}{\|\mathbf{x} - \mathbf{c}_i\|_2}, \quad i = 1 \dots k$$

- RootSift (“ \sqrt{SIFT} ”)³



¹ [Jégou, Perronnin, Douze, Sanchez, Pérez, Schmid. PAMI 2012]

² [Delhumeau, Gosselin, Jégou, Pérez. ACM MM 2013]

³ [Arandjelovic, Zisserman. CVPR 2013]



Exhaustive search

- Comparisons to BoW on Holidays (1500 images with relevance GT)

| Image signature | dim | mAP (%) |
|----------------------|---------|---------|
| BoW-20K | 20,000 | 43.7 |
| BoW-200K | 200,000 | 54.0 |
| VLAD-64 | 8192 | 51.8 |
| + $\alpha = 0.2$ | | 54.9 |
| + \sqrt{SIFT} | | 57.3 |
| + RN | | 63.1 |
| + LCS | | 65.8 |
| + <i>dense SIFTs</i> | | 76.6 |



Getting short and compact

- Towards large scale search
 - PCA reduction of image signature to $D' = 128$
 - Very fine quantization with *Product Quantizer* (PQ)*
 - Results on *Oxford105K* and *Holydays+1M* Flickr distractors

| Image signature | Ox105K | Hol+1M |
|-------------------------|--------|--------|
| Best VLAD-64 (8192 dim) | 45.6 | — |
| Reduced (128 dim) | 26.6 | 39.2 |
| Quantized (16 bytes) | 22.2 | 32.3 |

*[Jégou, Douze, Schmid. PAMI 2010]

Quantized signatures

- Vector quantization on k_f values

$$\mathbf{w} \approx q(\mathbf{w})$$

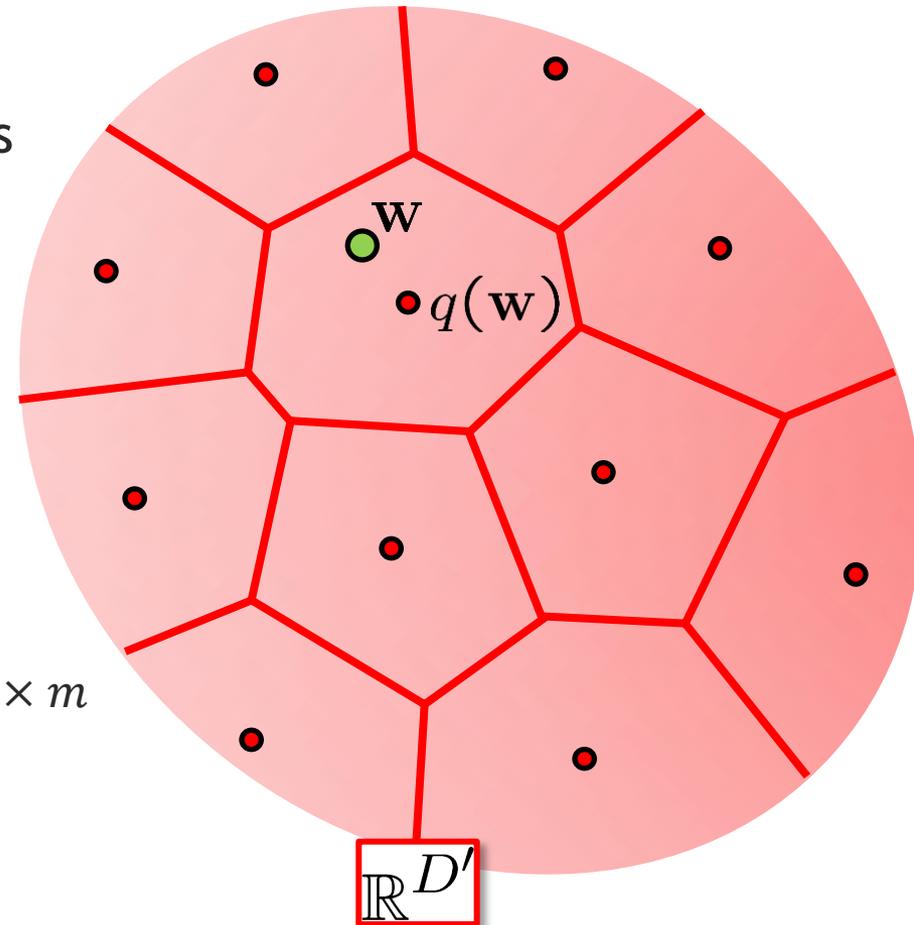
- For good approximation, large codes
 - e.g., 128 bits ($k_f = 2^{128}$)

- Practical with *product quantizer**

$$\mathbf{w} = \begin{bmatrix} \mathbf{w}_1 \\ \vdots \\ \mathbf{w}_m \end{bmatrix}, \quad q(\mathbf{w}) = \begin{bmatrix} q_1(\mathbf{w}_1) \\ \vdots \\ q_m(\mathbf{w}_m) \end{bmatrix}$$

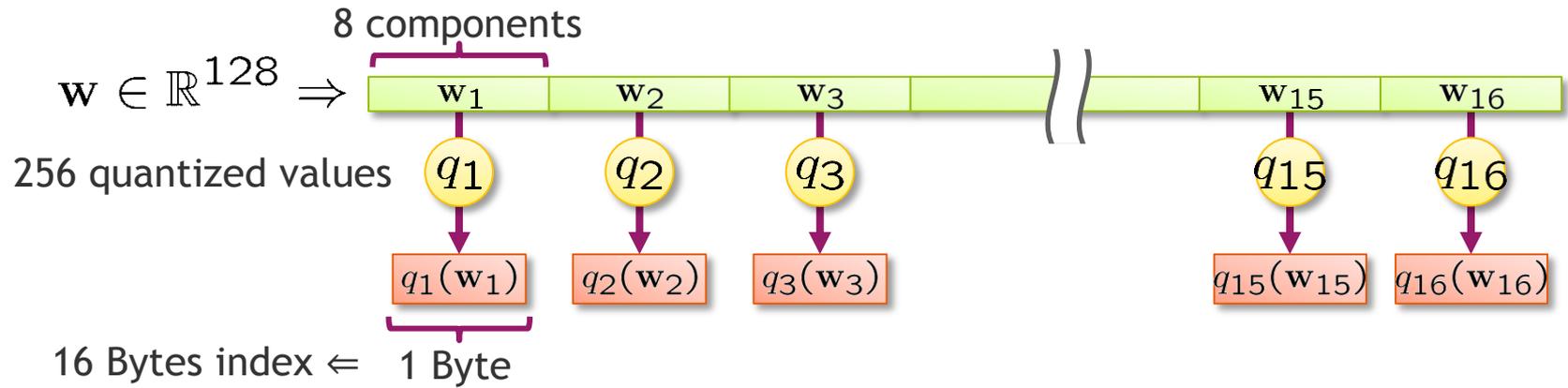
with k_r values per sub-quantizer

- yields $k_f = (k_r)^m$ with complexity $k_r \times m$



*[Jégou, Douze, Schmid. PAMI 2010]

Quantized signatures



$$\begin{aligned} D' &= 128 \\ m &= 16 \\ k_r &= 2^8 \\ k_f &= 2^{128} \end{aligned}$$

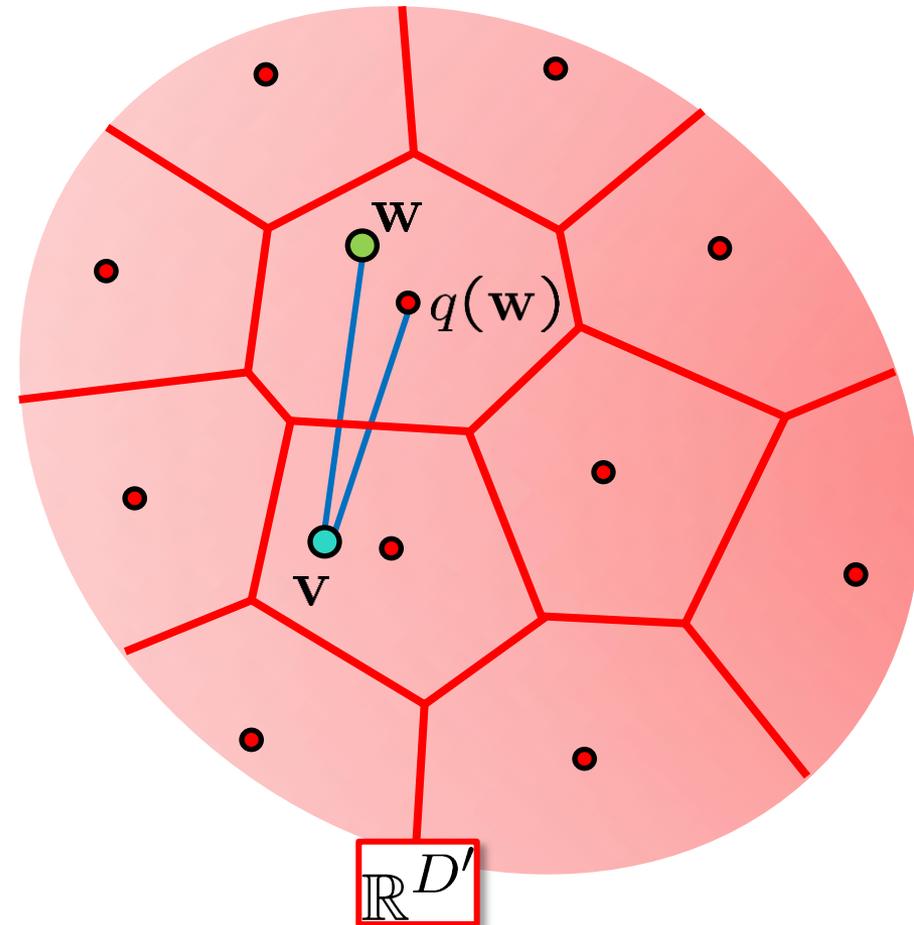
Asymmetric Distance Computation (ADC)

- Given query signature \mathbf{v} , distance to a basis signature \mathbf{w} :

$$\|\mathbf{v} - \mathbf{w}\|^2 \approx \sum_{i=1}^m \underbrace{\|\mathbf{v}_i - q_i(\mathbf{w}_i)\|^2}_{k_r \text{ possible values}}$$

- Exhaustive search among N_b basis images

mk_r distances + $(m - 1)N_b$ sums



ADC with Inverted Files (IVF-ADC)

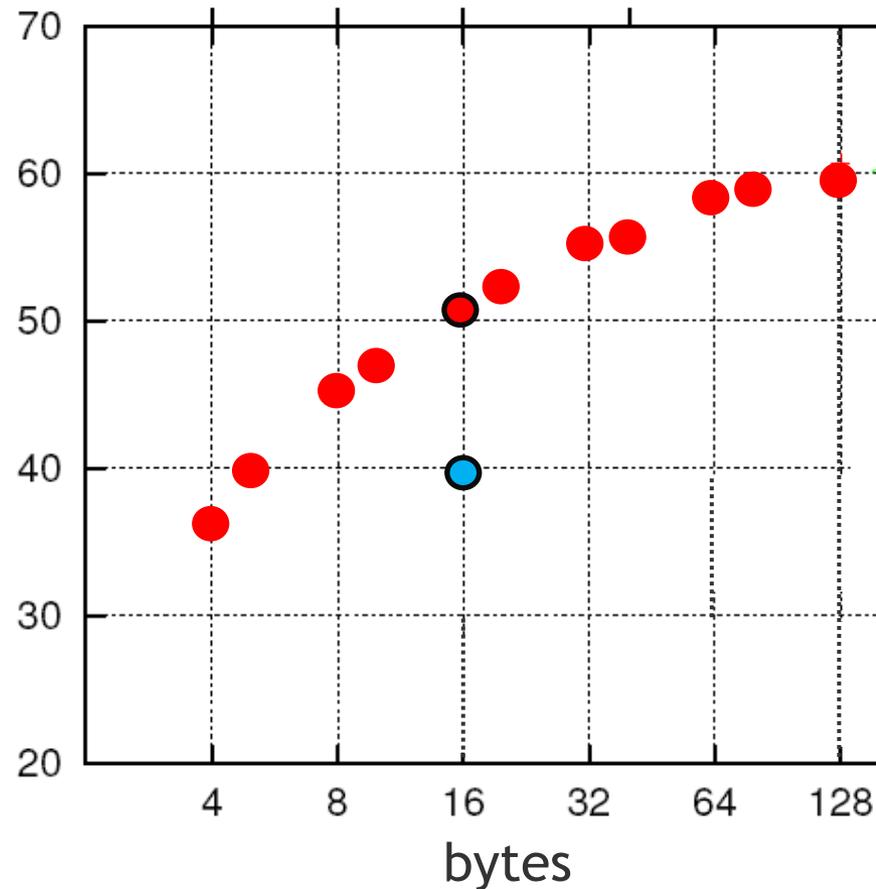
- Two-level quantization of signatures
 - Coarse quantization (e.g., $k_c = 2^8$ values)
 - One inverted list per code-vector
 - Compare only within lists of w nearest code-vectors to query
 - Fine PQ quantization of *residual* signatures (e.g., $k_f = 2^{128}$)
- Search among N_b basis images

$$mk_r \text{ distances} + w(m-1)N_b k_c^{-1} \text{ sums}$$

$w = 16, m = 16, k_r = k_c = 256 \Rightarrow$ one sum only per image with almost no accuracy change!

Performance w.r.t. memory footprint

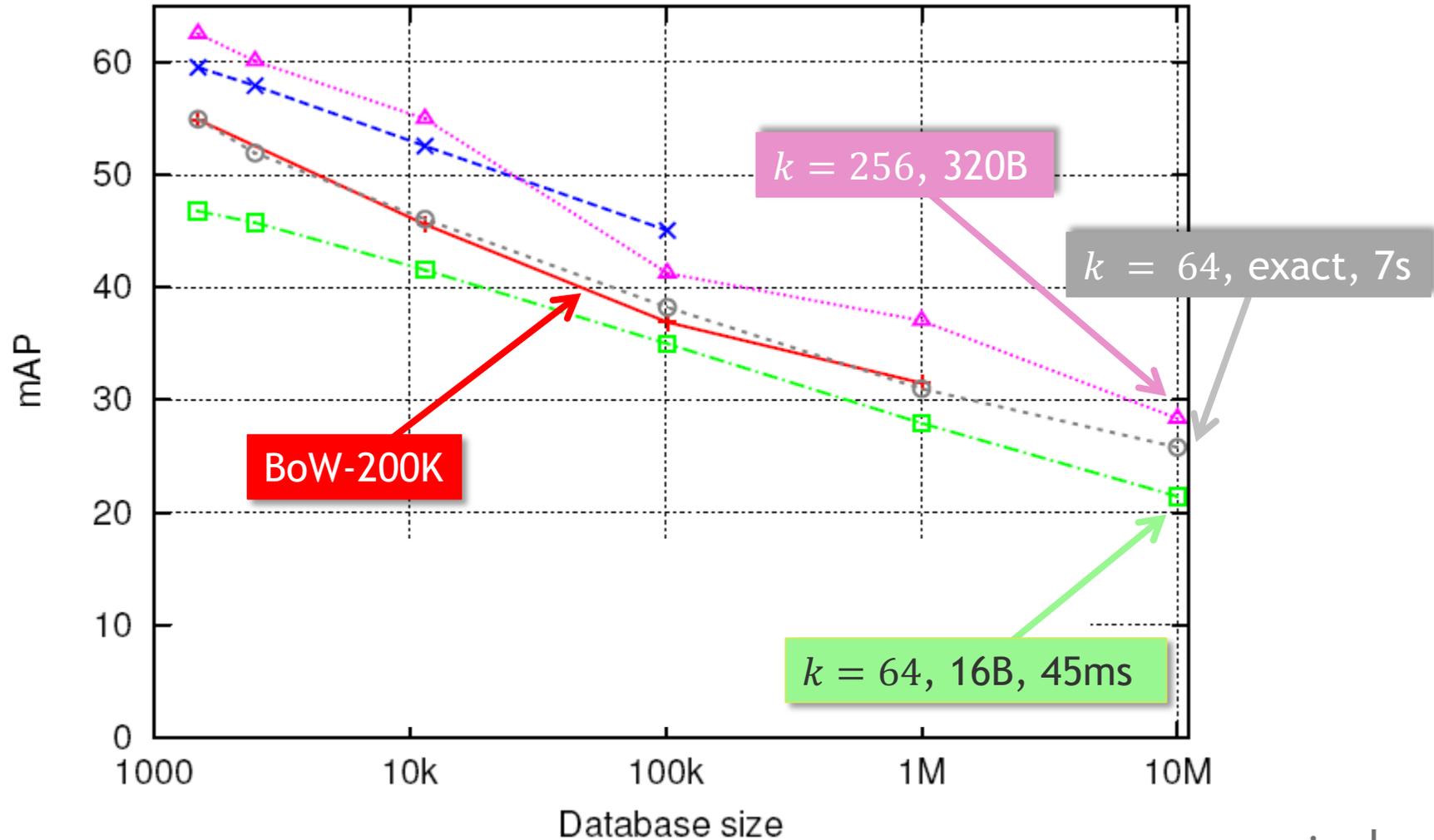
| Image signature | bytes | mAP (%) |
|------------------------------|--------|---------|
| BoW-20K | 10,364 | 43.7 |
| BoW-200K | 12,886 | 54.0 |
| FV-64 | | 59.5 |
| ▪ Spectral Hashing* 128 bits | 16 | 39.4 |
| ▪ PQ, $m = 16, k_r = 256$ | 16 | 50.6 |



*[Weiss *et al.* NIPS 2008]

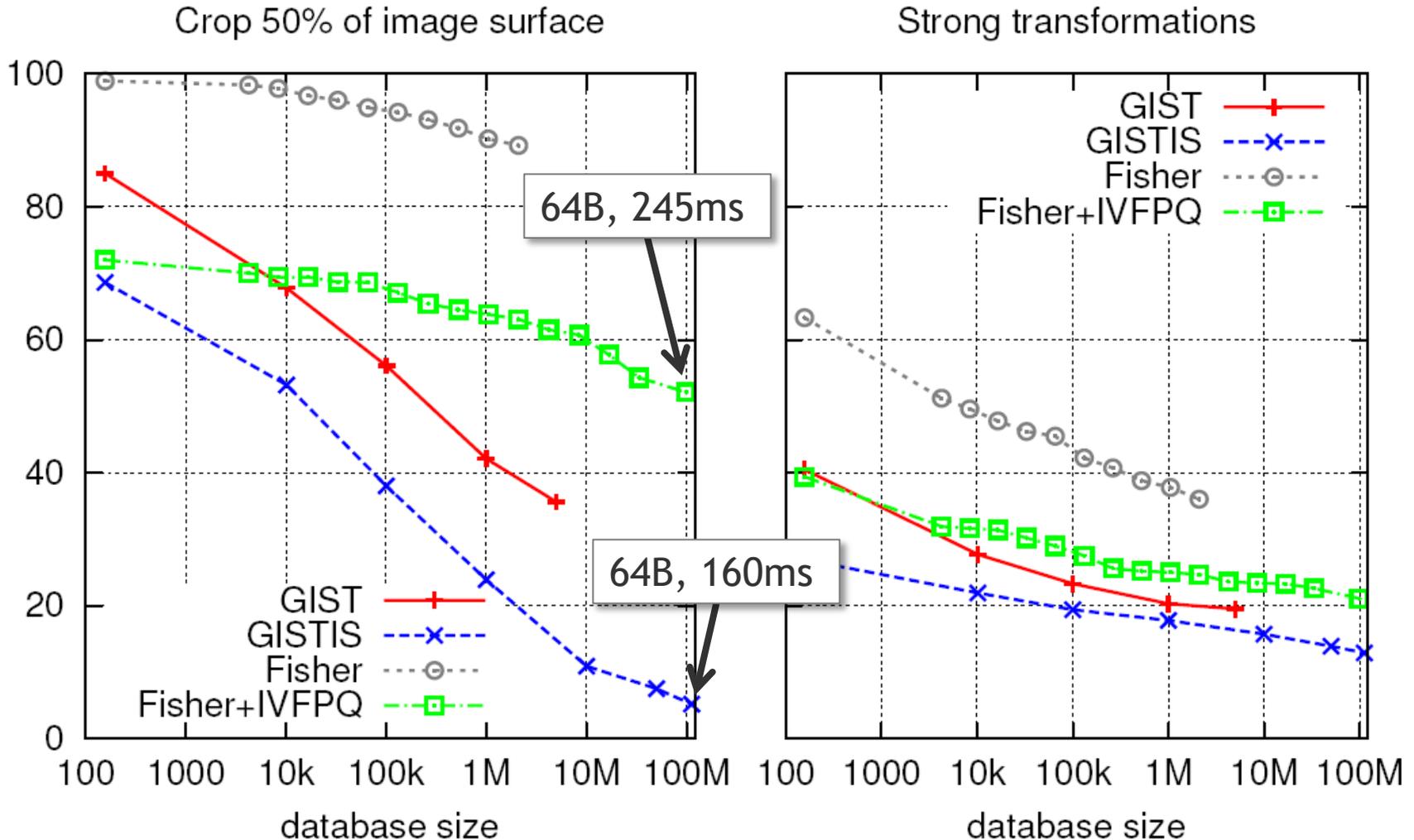
Large scale experiments

- Holidays + up to 10M distractors from Flickr



Larger scale experiments

■ Copydays + up to 100M distractors from Exalead



[GIST: Oliva, Torralab. PBR 2006][GISTIS: Douze *et al.* AMC-MM 2009] technicolor



Beyond Euclidean distance

- Kernel-based similarities
 - Other better but costly kernels
 - For histogram-like signatures: Chi2, histogram intersection (HIK)
- *Explicit embedding* recently proposed for learning¹
 - Given PSD kernel function $K(\mathbf{x}, \mathbf{y}) = \langle \phi(\mathbf{x}), \phi(\mathbf{y}) \rangle$
 - Find an *explicit finite dim.* approximation of implicit feature map

$$K(\mathbf{x}, \mathbf{y}) \approx \langle \tilde{\phi}(\mathbf{x}), \tilde{\phi}(\mathbf{y}) \rangle$$

- Learn linear SVM in this new explicit feature space
- KCPA²: a flexible data-driven explicit embedding

$$[K(\mathbf{x}_i, \mathbf{x}_j)] = U \Lambda U^\top \approx U_{[E]} \text{diag}(\lambda_1, \dots, \lambda_E) U_{[E]}^\top, E < N$$

- What about search?

¹[Vedaldi, Zisserman. CVPR 2010][Perronnin *et al.* CVPR 2010]

²[Schölkopf *et al.* ICANN 1997]

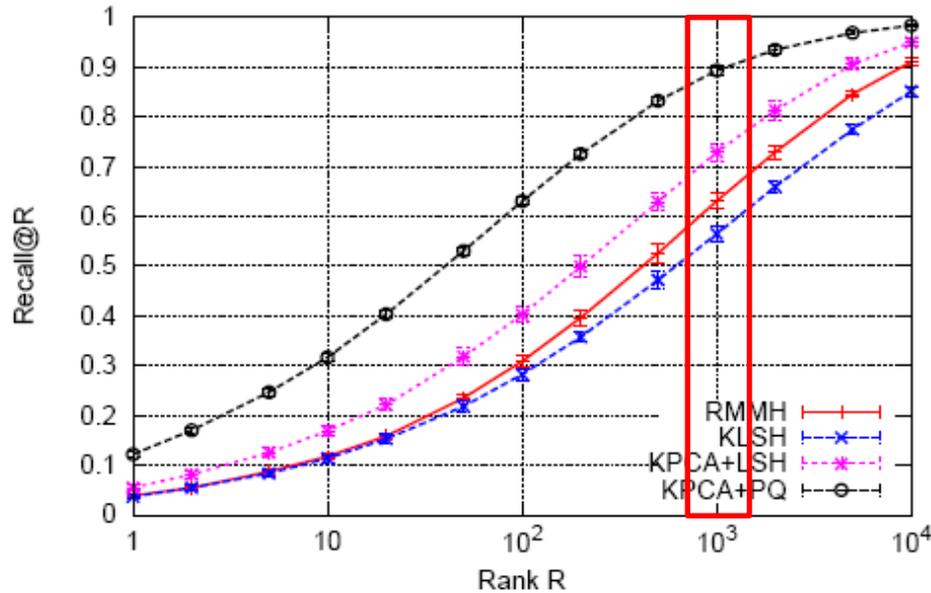
Approximate search with short codes

- Simple proposed approach* (“KPCA+PQ”)
 - Embed database vectors with learned KPCA
 - Efficient Euclidean ANN with PQ coding
 - Kernel-based re-ranking in original space
- Competitors: binary search in implicit space
 - Kernelised Locally Sensitive Hashing (KLSH) [Kulis, Grauman. ICCV09]
 - Random Maximum Margin Hashing (RMMH) [Joly, Buisson. CVPR11]
- Experiments
 - Data: 1.2M images from ImageNet with BoW signatures
 - Chi2 similarity measure
 - Tested also: “KPCA+LSH”(binary search in explicit space)

*[Bourrier, Perronnin, Gribonval, Pérez, Jégou. TR 2012]

Results averaged over 10 runs

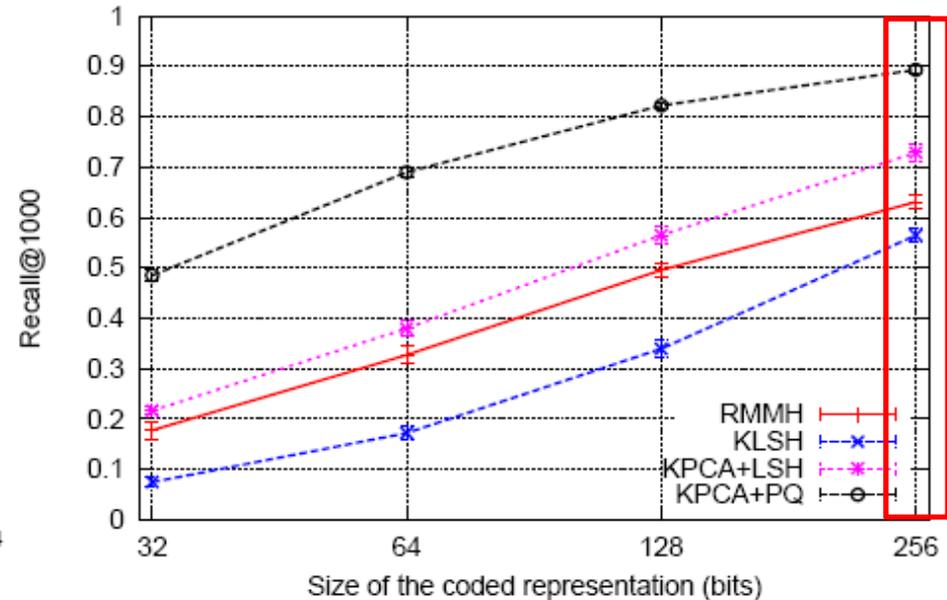
Imagenet (1000-D BOW, 1.261 million images)



Recall@R

$E = 128, B = 256 \text{ bits}, M = 1024$

Imagenet (1000-D BOW, 1.261 million images)

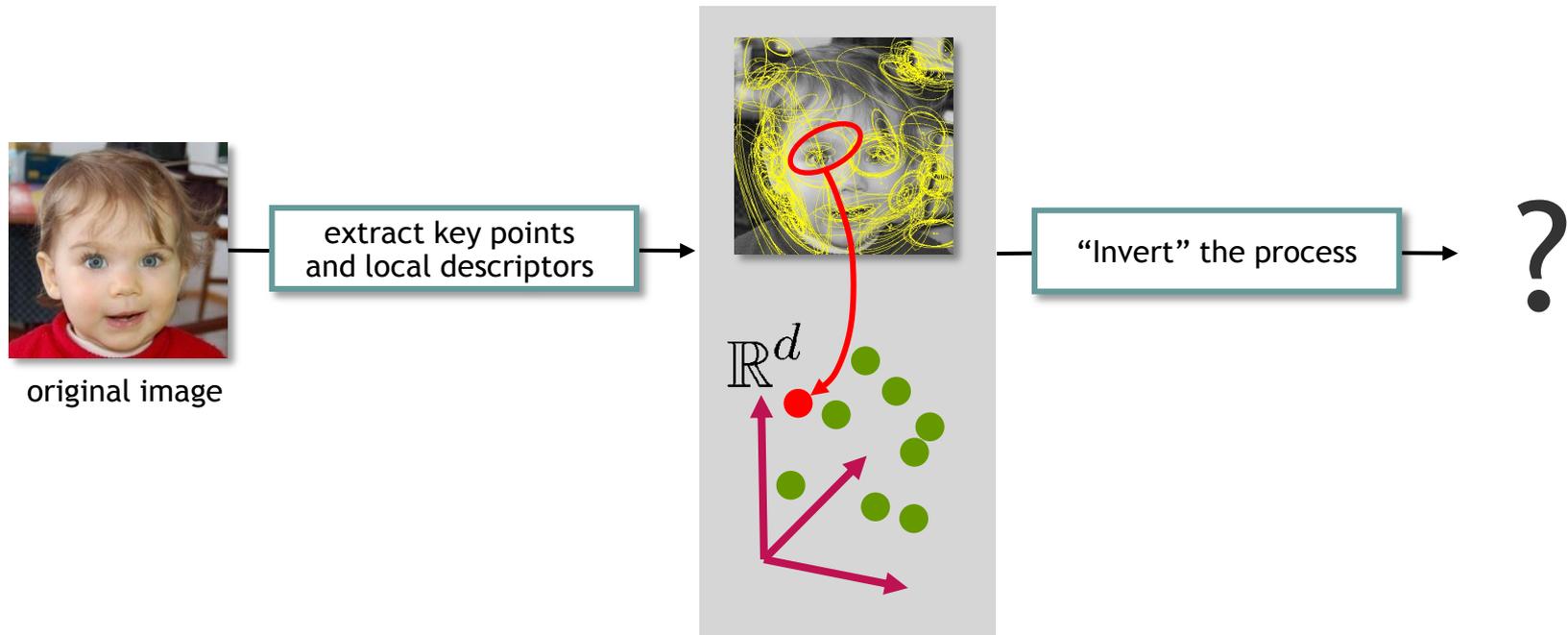


Recall@1000

$B = 32 \rightarrow 256 \text{ bits}$

Reconstructing an image from descriptors

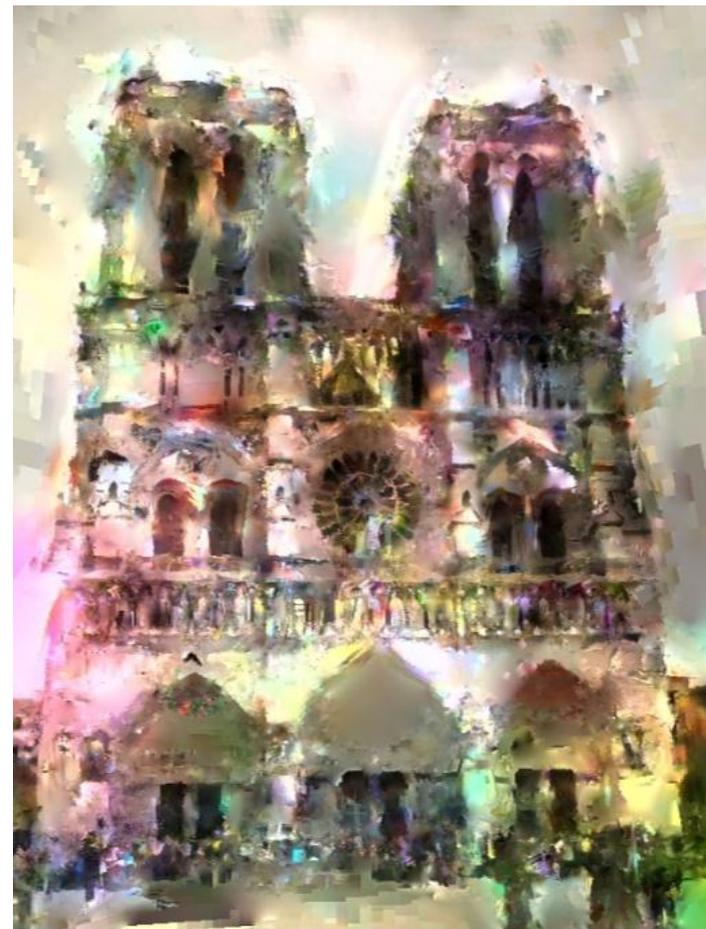
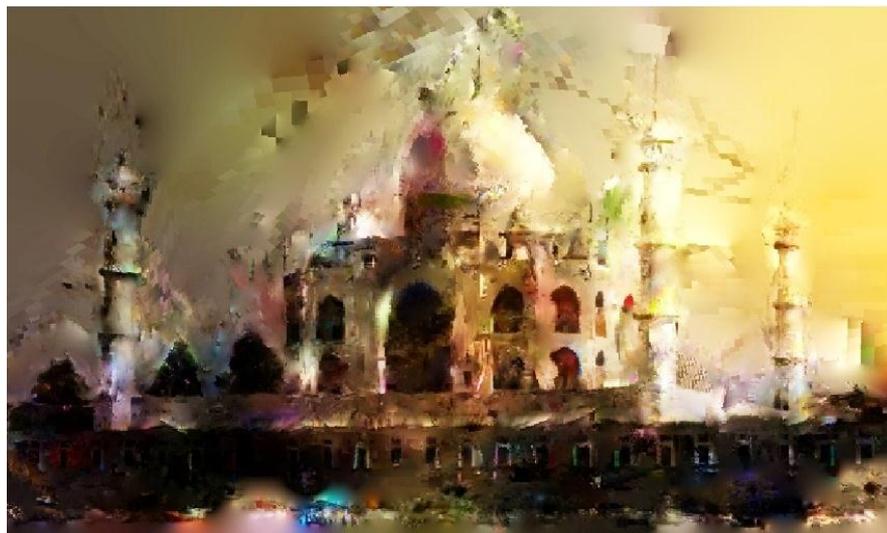
- If sparse local descriptors only are known



- Better insight into what local descriptors capture, with multiple applications

Reconstructing an image from descriptors

- Possible to some extent

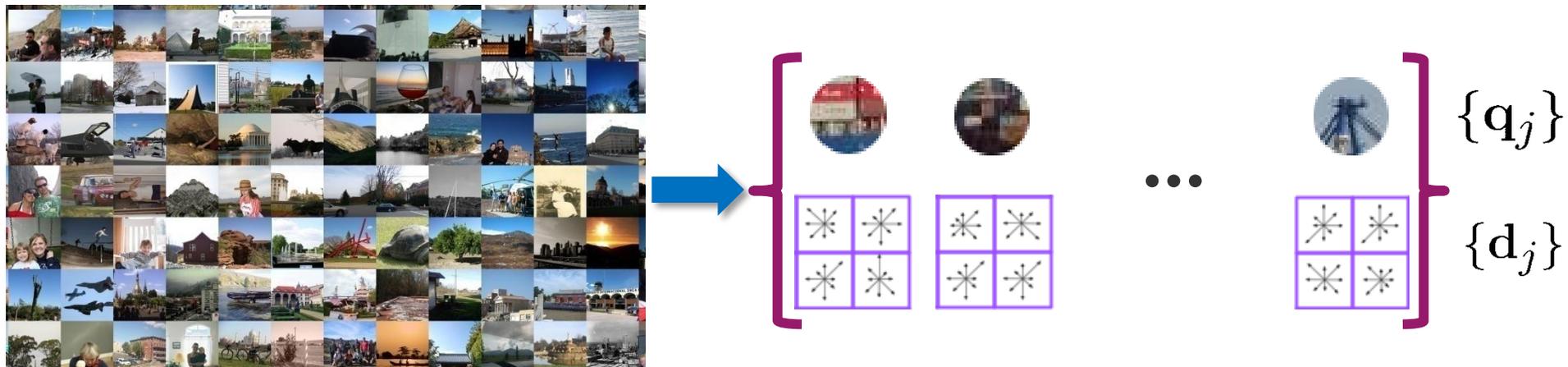


[Weinzaepfel, Jégou, Pérez. CVPR'2011]



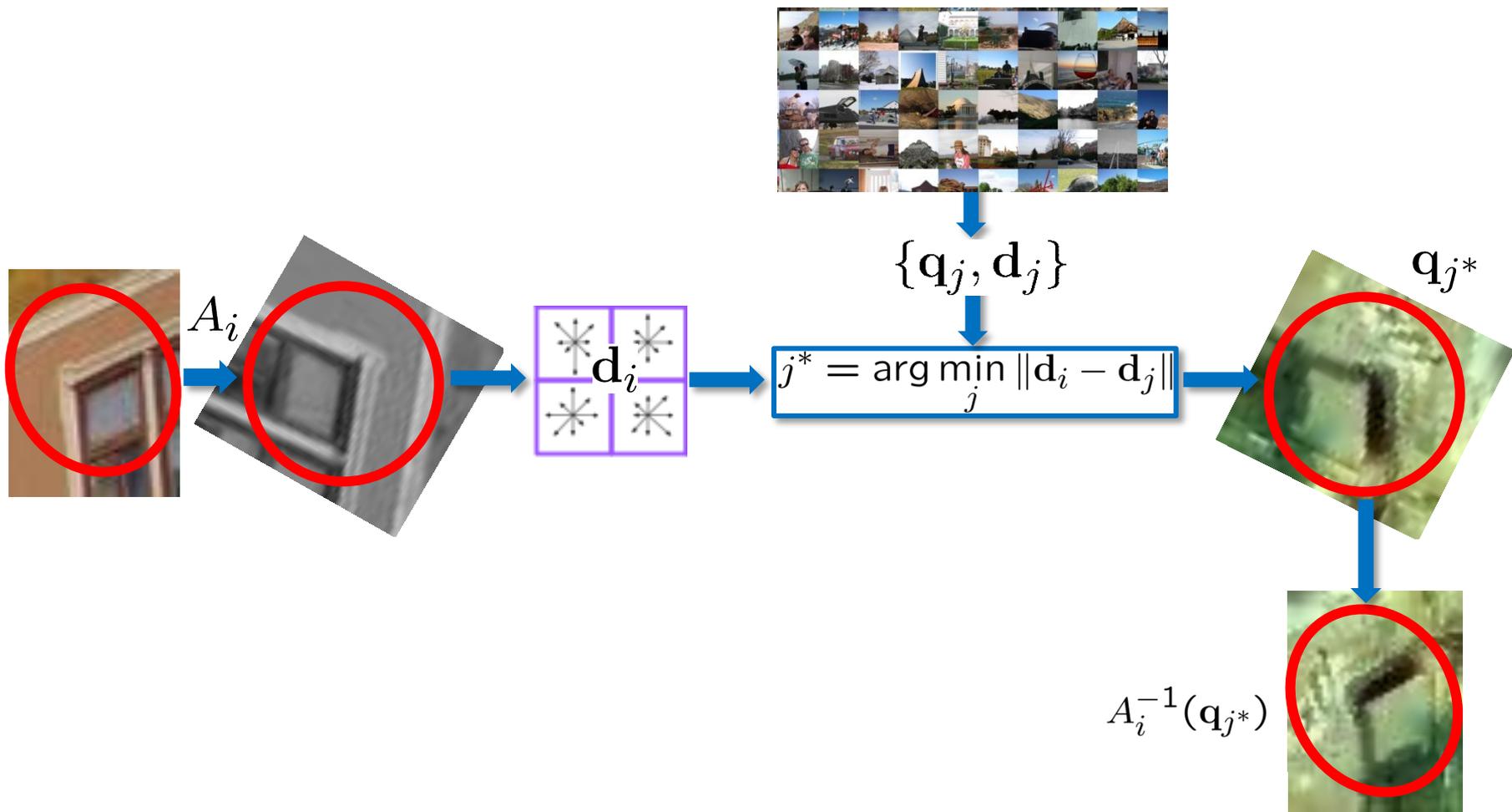
Inverting local description

- Local description, severely lossy by construction
 - Color, absolute intensity, spatial arrangement in each cell are lost
 - Non-invertible many-to-one map
 - Example-based regularization: *use key-points from arbitrary images*



- Patch collection must be large and diverse enough (e.g., 6M)

Inverting local description



Assembling recovered patches

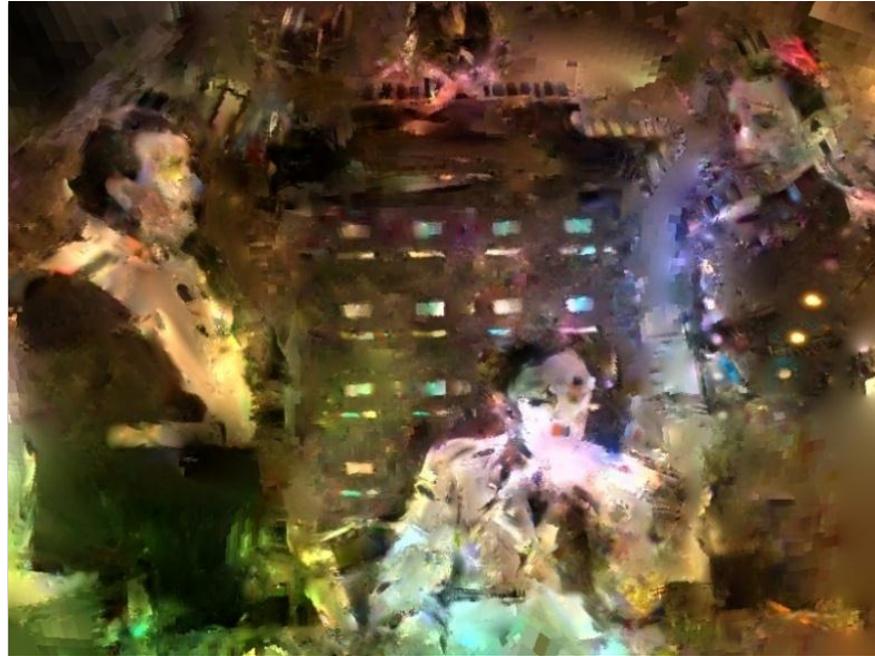
- Progressive collage
 - Dead-leaf procedure, largest patches first



- Seamless cloning*
 - Harmonic correction: smooth change to remove boundary discrepancies
- Final hole filling
 - Harmonic interpolation

*[Pérez, Gangnet, Blake. Siggraph 2003]

Reconstruction



Reconstruction

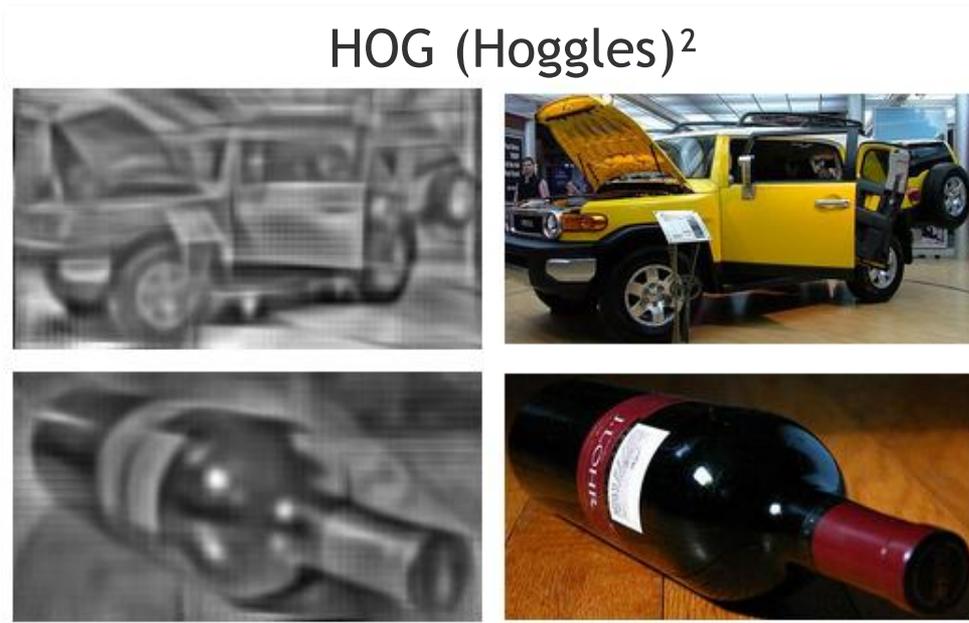


Reconstruction

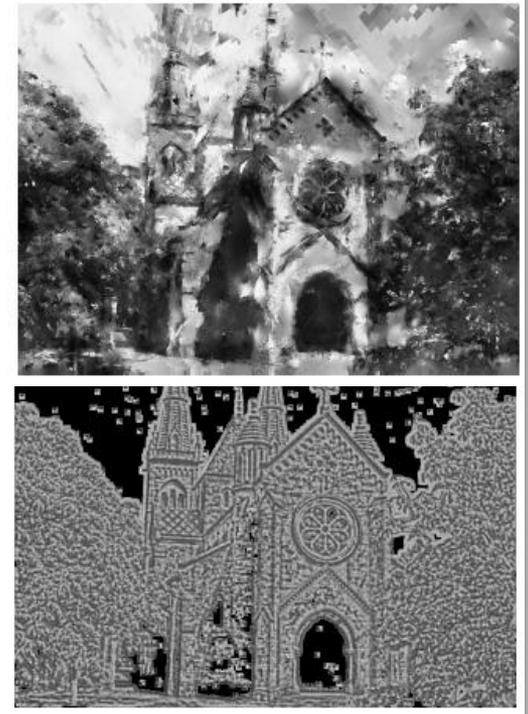


Outlook

- New: reconstruction from dense local features



local binary pattern¹



- Human-understandable images can be reconstructed
 - Visual insight into information exploited by detectors and classifiers
 - *Visual information leakage* in image indexing systems: privacy?

¹ [D'Angelo, Alahi, P. Vanderghenst. ICPR 2012]

² [Vondrick, Khosla, Malisiewicz, Torralba. ICCV 2013]